

$$1. \Delta G_v \text{ (bulk)}$$

o spherical nucleus

a) liquid-solid interfacial energy per unit

$$\Delta G = -\frac{4}{3}\pi r^3 \Delta G_v + 4\pi r^2 \gamma$$

$$I = f_0 N_0 \exp\left(-\frac{\Delta G^*}{kT}\right)$$

$$\ln I = \ln f_0 N_0 + \left(-\frac{\Delta G^*}{kT}\right)$$

$$\frac{\partial \Delta G}{\partial r} \Big|_{r^*} = 0 \Rightarrow r^* = \frac{2\gamma}{\Delta G_v}, \quad \Delta G^* = \frac{16}{3}\pi \frac{\gamma^3}{(\Delta G_v)^2}$$

$$n^* = \frac{32\pi}{3V} \left(\frac{\gamma}{\Delta G_v}\right)^3 \quad \left(\frac{4}{3}\pi r^3 = nV\right)$$

o The slope of  $\ln I$  vs.  $1/T$  at  $113^\circ\text{C} = -23.8 \times 10^3 \text{K} = -\frac{\Delta G^*}{k} (1.38 \times 10^{-23} \text{J/K})$

$$\Delta G^* = -3.2841 \times 10^{-19} \text{J}$$

$$= \frac{16}{3}\pi \frac{\gamma^3}{(\Delta G_v)^2}$$

$$\therefore \gamma^3 = -3.2841 \times 10^{-19} \times \frac{3}{16} \times \frac{1}{\pi} \times (10^8 \text{J m}^{-3})^2$$

$$\gamma = 0.0581 \text{ J m}^{-2}$$

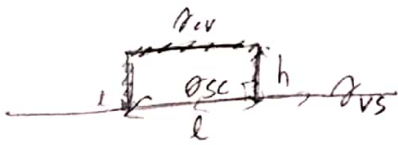
b)  $r^*$

$$r^* = \frac{2\gamma}{\Delta G_v} = \frac{2 \cdot 0.0581 \text{ J m}^{-2}}{+10^8 \text{ J m}^{-3}} = 1.1618 \times 10^{-9} = 1.1618 \text{ nm}$$

c)  $n^* = \frac{32\pi}{3V} \left(\frac{\gamma}{\Delta G_v}\right)^3, \quad V = V_m = \frac{4}{3}\pi r_{\text{tin}}^3 = \frac{4}{3}\pi \cdot (1.5 \times 10^{-10})^3 = 1.414 \times 10^{-29} \text{ m}^3$

$$= \frac{32\pi}{3 \times (1.414 \times 10^{-29})} \times \left(\frac{0.0581}{10^8}\right)^3 = \underline{\underline{46571}}$$

2.



$$\begin{aligned} \gamma_{vs} &= \gamma_{sc} + \gamma_{cv} \cos \theta \quad (\theta = 90^\circ) \\ &= \gamma_{sc} \end{aligned}$$

$$\Delta G = -V_{\text{cube}} \cdot \Delta G_v + \sum A_i \sigma_i$$

$$= -V_{\text{cube}} \cdot \Delta G_v + 4 \cdot l \cdot h \cdot \gamma_{cv} + l^2 \gamma_{cv} + l^2 \gamma_{sc} - l^2 \gamma_{vs}$$

$$= -l^2 h \cdot \Delta G_v + 4 \cdot l h \gamma_{cv} + l^2 \gamma_{cv} + l^2 \gamma_{sc} - l^2 \gamma_{sc}$$

$$\frac{\partial \Delta G}{\partial h} = 0, \quad \frac{\partial \Delta G}{\partial l} = 0$$

$$\frac{\partial \Delta G}{\partial h} = -l^2 \Delta G_v + \gamma_{cv} (4l) = 0$$

$$l^2 \Delta G_v - 4l \gamma_{cv} = 0$$

$$l(l \Delta G_v - 4 \gamma_{cv}) = 0$$

$$\Rightarrow \boxed{l^* = \frac{4 \gamma_{cv}}{\Delta G_v}}$$

$$\frac{\partial \Delta G}{\partial l} = -2lh \cdot \Delta G_v + 4h \gamma_{cv} + 2l \gamma_{cv} = 0$$

$$\downarrow l = l^*$$

$$= -\frac{8 \gamma_{cv}}{\Delta G_v} \cdot \Delta G_v \cdot h + 4h \gamma_{cv} + \frac{8 \gamma_{cv}}{\Delta G_v} \cdot \gamma_{cv}$$

$$= -4h \gamma_{cv} + 8 \frac{\gamma_{cv}^2}{\Delta G_v} = 0$$

$$\Rightarrow \boxed{h^* = \frac{2 \gamma_{cv}}{\Delta G_v}}$$

$$\Delta G^* = -l^* h \cdot \Delta G_v + 4 \cdot l^* h \gamma_{cv} + l^{*2} \gamma_{cv}$$

$$= -\frac{16 \gamma_{cv}^2}{\Delta G_v^2} \cdot \frac{2 \gamma_{cv}}{\Delta G_v} \cdot \Delta G_v + \gamma_{cv} \left( \frac{16 \gamma_{cv}}{\Delta G_v} \cdot \frac{2 \gamma_{cv}}{\Delta G_v} + \frac{16 \gamma_{cv}^2}{\Delta G_v^2} \right)$$

$$= -\frac{32 \gamma_{cv}^3}{\Delta G_v^2} + \frac{48 \gamma_{cv}^3}{\Delta G_v^2} = \boxed{\frac{16 \gamma_{cv}^3}{\Delta G_v^2}}$$