

AMSE205 Thermodynamics I

due Date: Apr. 22, 2006

Problem Set #3

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1. A rigid container is divided into two compartments of equal volume by a partition. One compartment contains 1 mole of ideal gas A at 1 atm, and the other compartment contains 1 mole of ideal gas B at 1 atm.
 - (a) Calculate the entropy increase in the container if the partition between the two compartments is removed.
 - (b) If the first compartment had contained 2 moles of ideal gas A, what would have been the entropy increase due to gas mixing when the partition was removed?
 - (c) Calculate the corresponding entropy changes in each of the above two situations if both compartments had contained ideal gas A.

2. A system containing 500 particles and 15 energy levels is in the following macrostate:

$$\{14, 18, 27, 38, 51, 78, 67, 54, 32, 27, 23, 20, 19, 17, 15\}$$

This system experiences a process in which the number of particles in each energy level changes by the following amounts:

$$\{0, 0, -1, -1, -2, 0, +1, +1, +2, +2, +1, 0, -1, -1, -1\}$$

Estimate the change in entropy for this process

3. 길이가 a 인 N 개의 막대꼴 분자가 쇠사슬과 비슷한 모양으로 연이어 이어져 있다. 이때 이웃한 두 분자의 상태는 완전히 겹쳐서 두 분자의 길이가 a 가 되거나 완전히 퍼져서 길이가 $2a$ 가 되는 두 가지 상태만 가능하다고 하자. 이웃하는 두 분자의 겹친 상태에서의 상호작용 에너지는 ε ($\varepsilon > 0$)이고, 퍼졌을 때는 0이라 하고, 이웃하지 않는 분자 사이에는 상호작용이 없다고 가정하자. 온도가 T 일 때 이 분자들의 평균 길이는 얼마인가?
(hint: 가장 짧은 때의 길이는 a 이고 에너지는 $(N-1)\varepsilon$ 이다.)
4. Text (Gaskell), Problem 4-3.

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Problem Set #2

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5. Derive the following, widely used thermodynamic equations.

(a) First TdS equation :
$$TdS = C_V dT + T \left(\frac{\partial P}{\partial T} \right)_V dV$$

(b) Second TdS equation :
$$TdS = C_P dT - T \left(\frac{\partial V}{\partial T} \right)_P dP$$

(c) First energy equation:
$$\left(\frac{\partial U}{\partial V} \right)_T = T \left(\frac{\partial P}{\partial T} \right)_V - P$$

(d) Second energy equation:
$$\left(\frac{\partial U}{\partial P} \right)_T = -T \left(\frac{\partial V}{\partial T} \right)_P - P \left(\frac{\partial V}{\partial P} \right)_T$$