



$$\Rightarrow \left. \frac{dG_m^\alpha}{dx_B} \right|_{x_B=x_B^\alpha} = \left. \frac{dG_m^\beta}{dx_B} \right|_{x_B=x_B^\beta}$$

$$\begin{cases} G_m^\alpha = x_A^\alpha G_A^\alpha + x_B^\alpha G_B^\alpha + RT(x_A^\alpha \ln x_A^\alpha + x_B^\alpha \ln x_B^\alpha) + x_A^\alpha x_B^\alpha L_{A,B}^\alpha \\ G_m^\beta = x_A^\beta G_A^\beta + x_B^\beta G_B^\beta + RT(x_A^\beta \ln x_A^\beta + x_B^\beta \ln x_B^\beta) + x_A^\beta x_B^\beta L_{A,B}^\beta \end{cases}$$

since, $\begin{cases} x_B^\alpha + x_A^\alpha = 1 \\ x_B^\beta + x_A^\beta = 1 \end{cases} \Rightarrow \begin{cases} x_A^\alpha = 1 - x_B^\alpha \\ x_A^\beta = 1 - x_B^\beta \end{cases}$

$$\begin{cases} G_m^\alpha = (1-x_B^\alpha) G_A^\alpha + x_B^\alpha G_B^\alpha + RT((1-x_B^\alpha) \ln(1-x_B^\alpha) + x_B^\alpha \ln x_B^\alpha) + (1-x_B^\alpha)x_B^\alpha L_{A,B}^\alpha \\ G_m^\beta = (1-x_B^\beta) G_A^\beta + x_B^\beta G_B^\beta + RT((1-x_B^\beta) \ln(1-x_B^\beta) + x_B^\beta \ln x_B^\beta) + (1-x_B^\beta)x_B^\beta L_{A,B}^\beta \end{cases}$$

$$\left. \frac{dG_m^\alpha}{dx_B} \right|_{x_B=x_B^\alpha} = \left. \frac{dG_m^\beta}{dx_B} \right|_{x_B=x_B^\beta}$$

$$-\cancel{G_A^\alpha} + \cancel{G_A^\alpha} + RT(-\ln(1-x_B^\alpha) - 1 + \ln x_B^\alpha + 1) + (1-x_B^\alpha) L_{A,B}^\alpha - x_B^\alpha L_{A,B}^\alpha$$

$$= -\cancel{G_A^\beta} + \cancel{G_A^\beta} + RT(-\ln(1-x_B^\beta) - 1 + \ln x_B^\beta + 1) + (1-x_B^\beta) L_{A,B}^\beta - x_B^\beta L_{A,B}^\beta$$

$$\hookrightarrow RT \ln \frac{x_B^\alpha}{1-x_B^\alpha} + (1-2x_B^\alpha) L_{A,B}^\alpha = RT \ln \frac{x_B^\beta}{1-x_B^\beta} + (1-2x_B^\beta) L_{A,B}^\beta$$

\Rightarrow Reference state 이 무관하게 상평형점 조건은 같음.