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# Thermodynamics

## Thermodynamics of CVD

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## Scope

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### CVD

1. Too much changeable results depending on the condition
2. Beyond Scientific Explanation for long time
3. Process development has been mostly empirical

### Approach (by Nong Moon Hwang, KRISS/SNU)

1. How to define the driving force of CVD
2. Low pressure synthesis of Diamond
3. Charged Cluster Model in CVD

### References

- ▶ N.M. Hwang et al., Diamond and Related Materials, 1 (1992) 191-194.; 3 (1993) 163-167.
- ▶ N.M. Hwang et al., J. Crystal Growth 135 (1994) 165-171; 143 (1994) 103-109; 160 (1996) 87-97; 160 (1996) 98-103; 162 (1996) 55-68.



## Homogeneous Nucleation

Nucleation of liquid from vapor  
assume spherical nucleus

$$dG = -S dT + V dP + \sum \mu_i dn_i + \gamma dA$$

at constant T, P

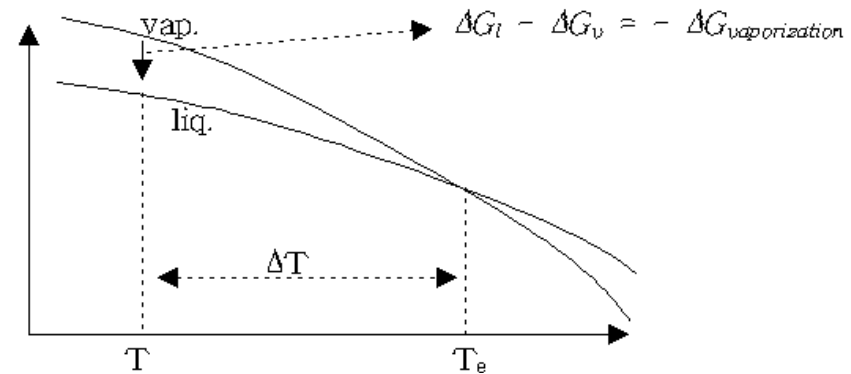
$$\begin{aligned} dG &= \mu_{vap} dn_{vap} + \mu_{liq} dn_{liq} + \gamma dA \\ &= -(\mu_{vap} - \mu_{liq}) dn_{liq} + \gamma dA \end{aligned}$$

set driving force,  $\Delta G_v = -(\mu_{liq} - \mu_{vap}) = \Delta G_{\text{vaporization}}$  (per volume of liquid)

$$\Delta G = -\frac{4}{3}\pi r^3 \Delta G_v + 4\pi r^2 \gamma$$

or if set molecular (atomic) volume,  $v$   
number of molecules (atoms) in cluster,  $n$

$$\Delta G = -n v \Delta G_v + (36\pi)^{\frac{1}{3}} n^{\frac{2}{3}} v^{\frac{2}{3}} \gamma$$



## Homogeneous Nucleation

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Critical size calculation

@ critical size

$$\left. \frac{\partial \Delta G}{\partial r} \right)_{r=r^*} = 0, \quad \left. \frac{\partial \Delta G}{\partial n} \right)_{n=n^*} = 0$$

$$\Rightarrow r^* = \frac{2\gamma}{\Delta G_v}, \quad \Delta G^* = \frac{16}{3} \pi \frac{\gamma^3}{(\Delta G_v)^2}$$

$$n^* = \frac{32\pi}{3v} \left( \frac{\gamma}{\Delta G_v} \right)^3$$

※  $\Delta G_{\text{vaporization}} = \Delta H_{\text{vaporization}} - T\Delta S_{\text{vaporization}}$

when assuming

$$\Delta H_{\text{vap}}(T) = \Delta H_{\text{vap}}(T_e)$$

$$\Delta S_{\text{vap}}(T) = \Delta S_{\text{vap}}(T_e)$$

$$\Delta G_{\text{vaporization}} = \Delta H_{\text{vap}} \cdot \Delta T / T_e$$

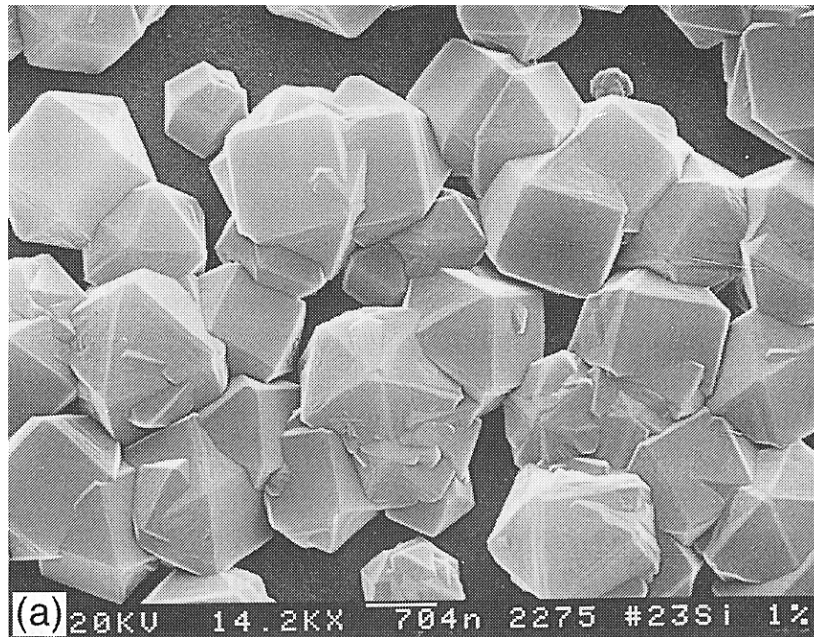
※ nucleation rate  $I = f_o N_o \exp(-\Delta G^*/kT) = f_o N_o \exp\left(-\frac{A}{(\Delta T)^2}\right)$

⇒ nucleation rate sharply increases over a very narrow Temperature range

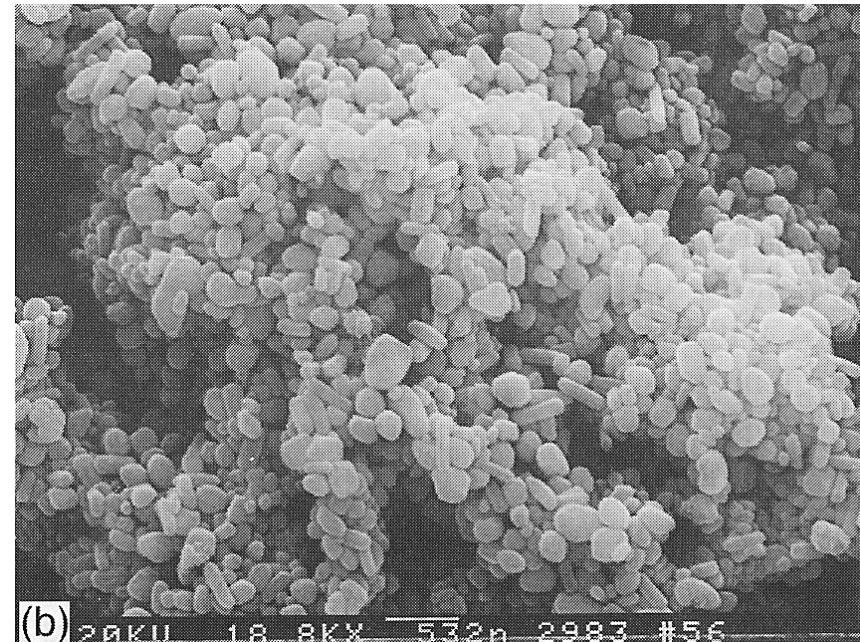


**CVD Diamond** - N.M. Hwang et al., J. Crystal Growth 162, 55 (1996)

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Diamond deposited on silicon substrate



Soot deposited on the iron substrate

# CVD Si - N.M. Hwang et al., J. Crystal Growth 218, 27 (2000)

W.S. Cheong et al. / Journal of Crystal Growth 218 (2000) 27–32

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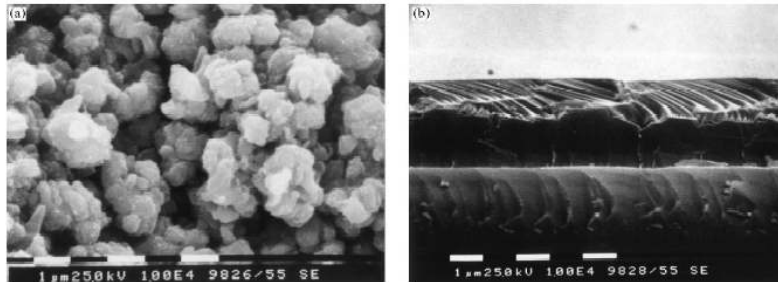


Fig. 1. SEM photographs of silicon deposits on (a) Fe and (b) Si substrates with the  $\text{SiH}_4 : \text{HCl} : \text{H}_2$  gas ratio of 1 : 1 : 98 under a react pressure of 1333 Pa at a substrate temperature of 1123 K.

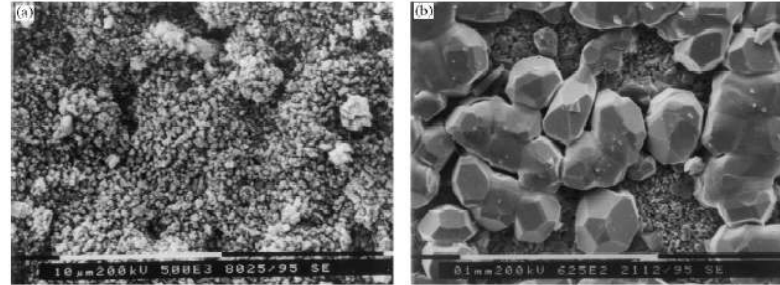


Fig. 4. SEM photographs of silicon deposits after (a) 3 and (b) 30 min on the Ni substrate with other conditions being the same as those for Fig. 1.

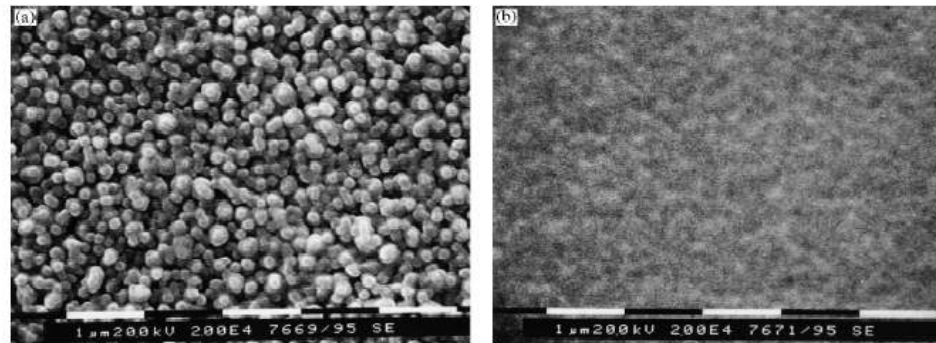


Fig. 3. SEM photographs of sputtered  $\text{Al}_2\text{O}_3$  films on (a) Fe and (b) Si substrates with a RF power of 100 W at a substrate temperature of 873 K under a reactor pressure of 2.7 Pa.



# CVD Si Nanowire - N.M. Hwang et al., J. Crystal Growth 218, 33 (2000)

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## Growth of silicon nanowires by chemical vapor deposition: approach by charged cluster model

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By the silicon CVD process using the gas ratio of  $\text{SiH}_4 : \text{HCl} : \text{H}_2 = 3 : 1 : 97$ , we were able to grow the silicon nanowires on Si,  $\text{SiO}_2$  and  $\text{Si}_3\text{N}_4$  substrates but not on Mo substrates. The growth mechanism of silicon nanowires was approached by the CCM. The highly anisotropic growth of nanowires could be explained by Coulomb interactions between nanowires and charged clusters, which tends to be attractive in the axial direction but repulsive in the radial direction.



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## Driving force of CVD Deposition

※ Example: Deposition of Silicon Carbide

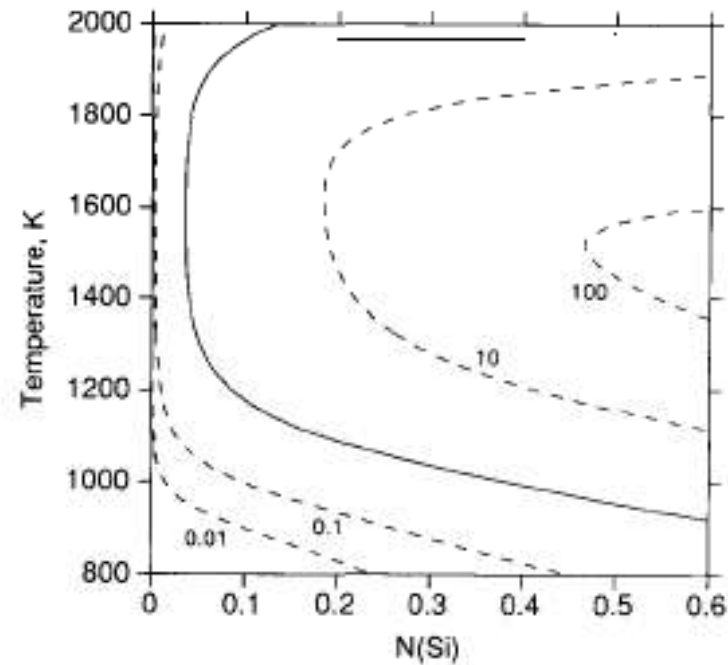
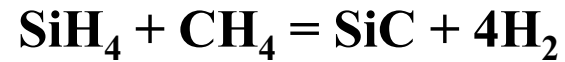


Fig. 1. CVD phase diagram of the Si-Cl-H system at 10666 Pa and composition of  $N(\text{H}) = 200$  and  $N(\text{Cl}) = 1$ . The dashed





## Thermodynamic Paradox

### Diamond formation with simultaneous graphite etching in low pressure synthesis of diamond

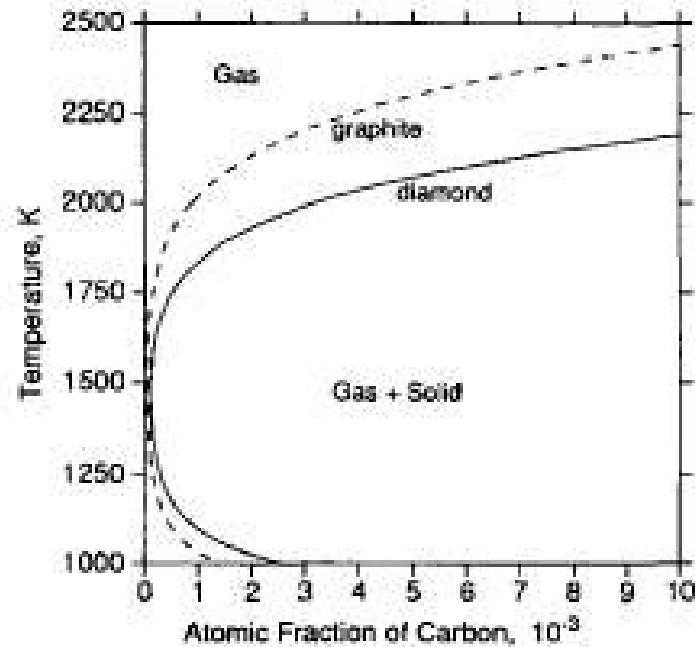


Fig. 1. The calculated CVD phase diagram of the C-H system at 2700 Pa. The dashed and the solid lines correspond to the solubility limit of carbon in the gas phase with respect to graphite and diamond, respectively.



## Nucleation of clusters in gas phase - Diamond/Graphite

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$$\Delta G = n\Delta\mu^{gas\rightarrow solid} + 4\pi\left(\frac{3\Omega}{4\pi}\right)^{2/3} n^{2/3}\sigma$$

$$I = q_o O_c \left(\frac{\Delta G^*}{kT}\right) \exp\left(-\frac{\Delta G^*}{kT}\right)$$

$$\frac{I^{dia}}{I^{gra}} = A \cdot \exp\left(\frac{\Delta G_{gra}^* - \Delta G_{dia}^*}{kT}\right)$$

$$\Delta G_{gra}^* - \Delta G_{dia}^* = \frac{16\pi \Omega_{gra}^2 \sigma_{gra}^3}{3(\Delta\mu^{gas\rightarrow gra})^2} - \frac{16\pi \Omega_{dia}^2 \sigma_{dia}^3}{3(\Delta\mu^{gas\rightarrow dia})^2}$$

The nucleation ratio is very sensitive to the variation of the surface energy ranging from  $10^{10}$  to  $10^{-6}$  with  $\sigma_{dia} = 3.7$  and  $4.1 \text{ J/m}^2$

at  $1200\text{K}$  and  $\sigma_{gra} = 3.1 \text{ J/m}^2$

→ There must be some factor that modifies the surface energy of diamond

→ **Creation of the *Charged Cluster Model***

